I. INTRODUCTION

With the LHC now gearing up for its high luminosity phase, all detectors will undergo substantial upgrades to cope with the expected high levels of pileup. The tracking detectors especially are an important component of this effort. ATLAS [1], CMS [2] and LHCb [3] are all aiming to incorporate tracking information as early on in the trigger decisions as possible, for the phase II upgrade or sooner. For CMS in particular, as of run 4, the modules in the outer tracker will consist of two closely spaced sensors, such that a rudimentary momentum measurement will be possible on a single module using the pairs of hits (stubs) [4]. A momentum preselection of $p_T > 2$ GeV on these track stubs then greatly reduces the occupancy, rendering preliminary track finding feasible under the stringent time constraints of the L1 trigger.

It has been shown recently that this approach can in fact reconstruct tracks with a transverse impact parameter up to roughly 10 cm, opening up the exciting possibility of a dedicated L1 trigger for long-lived particles (LLPs) [5]. Concretely, [6] showed that demanding a number of displaced tracks and a moderate scalar sum of the jet $p_T$ ($H_T$) of roughly 150 GeV can greatly increase the trigger efficiency for Higgs bosons decaying to a pair of displaced dijets. In this work we build on [5,6] by exploring the feasibility of a level-1 trigger for a low mass displaced exotics originating from heavy flavor decays. The method can also be applied to signatures without muons but with a moderate amount of missing transverse energy, $H_T$ or multiple displaced vertices in the event.

We show that the phase II upgrade of the CMS tracking detector could enable the experiment to trigger on very low mass $O(1$ GeV) displaced muon pairs with minimal $p_T$ cuts. As a result, CMS can be competitive with LHCb when searching for low mass displaced exotics originating from heavy flavor decays. The method can also be applied to signatures without muons but with a moderate amount of missing transverse energy, $H_T$ or multiple displaced vertices in the event.

II. TOY DETECTOR SIMULATION

A. Signal and background simulation

The example signal we consider is that of a light particle ($\phi$) produced through the $B \rightarrow X_s \phi$ decay with $\phi$ decaying to muons ($\phi \rightarrow \mu^+ \mu^-$) through a displaced vertex. Such a signal can arise from a light scalar mixing with the Higgs boson, which itself is a feature in many UV complete models of beyond the Standard Model physics. A model of this kind typically predicts correlations between the lifetime, production rate and branching ratios of the new particle, however in this work we simply parametrize the yield in terms of the lifetime ($\tau_\phi$) of $\phi$ and its production rate, expressed in terms of $Br[B \rightarrow X_s \phi] \times Br[\phi \rightarrow \mu^+ \mu^-]$, where $Br[B \rightarrow X_s \phi]$ is the inclusive $B$-meson branching...
TABLE I. Ranges used for simulation of fake tracks. Not all combination of parameters can produce four or more valid stubs. (See Fig. 8 in the Appendix.)

<table>
<thead>
<tr>
<th>Track parameter</th>
<th>Low range</th>
<th>High range</th>
</tr>
</thead>
<tbody>
<tr>
<td>$q/p_T$</td>
<td>$-1/(2 \text{ GeV})$</td>
<td>$1/(2 \text{ GeV})$</td>
</tr>
<tr>
<td>$\phi$</td>
<td>0</td>
<td>$2\pi$</td>
</tr>
<tr>
<td>$d_0$</td>
<td>$-14 \text{ cm}$</td>
<td>$14 \text{ cm}$</td>
</tr>
<tr>
<td>$\tan \lambda$</td>
<td>$-6$</td>
<td>$6$</td>
</tr>
<tr>
<td>$z_0$</td>
<td>$-15 \text{ cm}$</td>
<td>$15 \text{ cm}$</td>
</tr>
</tbody>
</table>

Two sources of background are considered, assuming an average of 200 pileup events. First, and largest, is the random crossings of fake (i.e., comprised of the unrelated stubs) tracks. We assume the number of fake tracks averages 30 per event, with all five track parameters (see e.g., [15]) $(q/p_T, \phi, d_0, \tan \lambda, \text{and } z_0)$ uniformly distributed. This assumption is based on estimates of the expected occupancy of the trigger system [2], and was reproduced by CMS with a full simulation [6]. Not all combinations of parameters produce tracks with observable stubs, mostly due to the anticorrelation between the $q/p_T$ and $d_0$ (see Fig. 8 in the Appendix). We throw uniformly distributed track parameters (see Table I) until we get a track that is expected to have at least four observable stubs.

The second source of background is the production of known long-lived particles, dominated by the $K_S$. We used inclusive QCD events generated with PYTHIA 8 [12,13] to estimate it.

We neglect interactions of prompt particles with the material of the detector, as they are relatively rare and are not expected to produce candidates that point back to the primary vertex (PV). High energy photon conversions point back to the PV, but are trivial to remove based on the smallness of the opening angle. In fact, it is likely that the vertex selection cuts in Sec. III remove most of them, though this is difficult to estimate with our toy simulation alone. It is therefore possible that a requirement on the opening angle will be needed, which could degrade the signal efficiency for very low mass $(m_\psi \ll 1 \text{ GeV})$.

B. Track reconstruction

The toy Monte Carlo to estimate track reconstruction and resolution is similar to the one in [5], with several important additions.

The toy tracker has six perfectly cylindrical double layers covering $|\eta| < 2.4$. Hits in the double layers produce a stub if the azimuthal offset between them is consistent with one from a prompt track with $p_T > 2 \text{ GeV}$. The hits are smeared according to the expected resolutions [4]. We also make a simple estimate of multiple scattering in the detector, assuming tracks change direction of travel when crossing a tracking layer by a random angle with mean of zero and Gaussian sigma of $4 \times 10^{-4}/p_T$ [4,16]. We do not consider the effects of small, non-Gaussian tails to the scattering distribution, since they are unimportant for the signal, and for background they can be viewed as a small contribution to the fake displaced tracks. To account for scattering in the pixel detector, we add scattering layers corresponding to approximate positions of the pixel layers.

The resulting hits are then fit to a five-parameter helical trajectory. Figure 1 shows the impact of the multiple scattering on the track impact parameter resolution for a signal sample with $m_\psi = 0.5 \text{ GeV}$. The reconstruction efficiency depends on the required number of stubs, the $p_T$ and the transverse impact parameter. For example, for tracks with four stubs, the efficiency is roughly 80% (50%) for transverse impact parameter of 5 cm (10 cm). For plots of the efficiency in various cases we refer the reader to Ref. [5].

C. Vertex reconstruction

The fitted tracks are the inputs to the vertex finding algorithm, which is deliberately kept as simple as possible, as proper vertexing is computationally prohibitive at the L1 trigger level. Our simplified vertex finder proceeds as follows: First we calculate the intersections between the two helices in the transverse plane. If no intersection exists, we identify the transverse location of the candidate vertex with the point on the line defined by the centers of the circles for which the distance to the circle boundaries is equal. The distance between both circle boundaries measured along this line is a measure of the quality of the vertex in the transverse plane, and is labeled by $\Delta_T$. We subsequently compute the distance between the tracks in the $z$ direction for this candidate vertex, which we denote by $\Delta_z$. If two intersections are found, we calculate the distance in the $z$ direction between both tracks ($\Delta_z$) for each of the two solutions, and select the solution for which $|\Delta_z|$ is smallest. The $\Delta_T$ variable is set to zero in this case.

Once a candidate vertex is found, we use its coordinates and the reconstructed track momenta to compute the impact parameter of the mother particle’s trajectory in the
transverse plane with respect to the origin ($d_T$). We further compute the angle ($\alpha_T$) in the transverse plane between the mother’s reconstructed trajectory and the line connecting the vertex location with the origin. Finally, we record the distance of the vertex from the origin, in the transverse plane ($R_T$). The above variables are summarized in the diagram in Fig. 2. Note that we use the origin of the CMS coordinate system as a reference point, rather than the primary vertex, since we do not assume we identified the primary vertex at the trigger level. Figure 3 shows the resolution of the reconstructed vertex radius, with and without multiple scattering, for $m_{\phi} = 0.5$ GeV.

### III. ANALYSIS AND RESULTS

Figures 4–6 show the distributions of $\Delta z$, $\cos \alpha_T$ and $d_T$ respectively, for the signal and for fake vertices. Based on these distributions, we define the following set of cuts:

(i) $d_0 > 1$ mm for each track
(ii) at least five stubs for one of the tracks, and at least four stubs for the other.
(iii) $\Delta_T < 0.2$ cm
(iv) $\Delta_z < 1.0$ cm
(v) $\cos \alpha_T < 0.9995$
(vi) $d_T < 0.1$ cm
(vii) $R_T > 1.5$ cm.

The cut on the track impact parameter $d_0$ in (i) prevents prompt tracks from contributing to the rate. The transverse size of the beam spot is negligible compared to the $d_0$ resolution of the track trigger (see Fig. 1). Cuts (ii) to (vi) are intended to suppress the contribution from fake tracks to the trigger rate. Of these (iv) and (v) provide roughly $10^{-2}$ background suppression each, as can be seen from Figs. 4 and 5. On the other hand, the background reduction from (ii) and (iii) combined is only $\sim 50\%$ and these cuts could in principle be omitted. The cuts on $d_T$ and $\alpha_T$ are rather strongly correlated, but some additional background suppression is nevertheless gained by imposing both, with
virtually no loss in signal efficiency (see Fig. 6). Finally, the
cut on the vertex radius in (vii) reduces the rate from
B-decays to the kHz level, though it is to a large degree
degenerate with the cuts on \( d_0 \).

The rates for finding a vertex satisfying the above criteria
are given in Table II for various \( p_T \) cuts on the tracks. Fake
vertices and \( K_S \) decay contribute roughly equally to the
trigger rate.\(^1\) As is, these rates are still too high for a realistic
trigger and an additional selection is therefore needed to
further reduce the rate with roughly 2 orders of magnitude.
Depending on the signature of interest, this could for
instance be an \( H_T \) or missing transverse energy (MET)
requirement, or a second displaced vertex in the event.

For our example, we require that both tracks are matched
to a track candidate in the muon detectors. The signal
efficiency for this requirement is difficult to model without
a full simulation and depends on the \( p_T \) threshold of the
muons. We therefore assume that the signal efficiency is a
step function with a 100% efficient plateau, but vary the
background rate is driven by the fake muon rate: If the rate
\( p_T \gtrsim 10 \) GeV thresholds for both muons \([17,18]\). As a
point of comparison, we loosely model the acceptance of
such a trigger by

\[ (i) \ |\eta| < 2.4 \text{ for both muons} \]
\[ (ii) \ p_T > 10 \text{ GeV for both muons} \]
\[ (iii) \ R_T < 600 \text{ cm}, \]

where the \( R_T \) cut is loosely based on geometry of the
ATLAS muon system. [For large lifetimes, the CMS yield
would be smaller by an \( O(1) \) factor, for identical truth-level
\( p_T \) thresholds.] We assume that this trigger is 100% efficient, which is conservative for the sake of our comparison. We further compare with the acceptance of LHCb,
following the discussion in \([11]\):

\[ (i) \ 2.0 < \eta < 5 \text{ for both tracks} \]
\[ (ii) \ p_T > 0.5 \text{ GeV for both tracks} \]
\[ (iii) \ 3\text{-momentum of both tracks larger than } 6 \text{ GeV} \]
\[ (iv) \ R_T < 2.2 \text{ cm} \]
\[ (v) \ z\text{-coordinate of vertex smaller 60 cm.} \]

The cuts on the vertex location are motivated by the geo-
metry of the VELO detector, however for the \( B \to X_s \phi \)
signature LHCb may reconstruct the \( \phi \) also somewhat
outside the VELO by triggering on the associated \( X_s \) state.
This can increase the LHCb efficiency with an \( O(1) \)
amount in the regime where the \( \phi \) predominantly decays
outside the VELO \([19]\). We assumed a total integrated
luminosity of 300 fb\(^{-1}\) for LHCb and 3 ab\(^{-1}\) for ATLAS
and CMS.

The resulting yield for all three strategies is shown in
Fig. 7 for two benchmark mass points, shown in terms of
the production rate and lifetime of \( \phi \). Given that the
suppression factor from the matching with the muon
system is unknown at this time, we show the results for
the CMS displaced vertex trigger for a few different \( p_T \)
thresholds on the muons. The (2,2) point in Table II was
hereby omitted, since muons this soft will not be recon-
structed by the muon chambers. With the assumptions
above, we find that CMS has the potential to improve on the
LHCb yield in the large \( cT \) regime. In the low \( cT \) regime
LHCb clearly performs better due to the better vertex
resolution of the VELO detector and LHCb’s capability to
do the full event reconstruction online.

Our proposed displaced vertex trigger is moreover highly
complementary to the standalone dimuon trigger (dashed
purple curve in Fig. 7); At high \( cT \) the standalone dimuon
trigger has much larger geometric acceptance than our

\begin{table}
\centering
\begin{tabular}{|c|c|c|}
\hline
Minimum \( p_T \) selection & Fakes & \( K_S \) \\
\hline
(2, 2) GeV & 0.050 & 0.114 \\
(3, 3) GeV & 0.025 & 0.020 \\
(4, 4) GeV & 0.015 & 0.006 \\
(5, 3) GeV & 0.021 & 0.005 \\
\hline
\end{tabular}
\caption{
Rates for events to have at least one vertex candidate, before the muon system requirements. Pileup of 200 is assumed.
}
\end{table}
displaced vertex trigger, however for soft signals, such as heavy flavor decays, this is offset by our lower $p_T$ requirements. For high energy signals from e.g., supersymmetric particles, the standalone dimuon trigger will continue to have the best efficiency.

It should be noted that all curves are each somewhat optimistic in different ways: For LHCb and the standalone dimuon trigger no detector smearing is attempted and the reconstruction is assumed to be 100% efficient. For the displaced vertex trigger we have assumed negligible losses in signal efficiency at the high level trigger. Given that the backgrounds in all cases are highly nontrivial and are best estimated from data, we do not attempt to project exclusion limits at this stage.

IV. DISCUSSION

We have performed a toy simulation of the future CMS track trigger for the heavy flavor benchmark $B \to X_s \phi$, where $\phi$ is a long-lived particle with an appreciable branching ratio to muons. The rate from random crossings of fake tracks and $K_S$ mesons can be brought under control by a combination of pointing cuts and by matching the tracks to activity in the muon chambers. The track trigger could allow CMS to compete with LHCb on soft, displaced signatures beyond the Standard Model physics, in particular in the context of exotic heavy flavor decays and dark photon models.

As mentioned above, at least two handles (pointing and muon matching) are needed to bring the rate from random track crossings down to an acceptable level for the high level trigger. There are therefore a number of possible variations on our strategy, by relaxing the pointing and/or muon requirements and instead demanding:

(i) A dimuon vertex without pointing but with a moderate amount of MET. This may be powerful for inelastic dark matter models.

(ii) Two reconstructed vertices in the event. This is of interest for e.g., hidden valley/dark shower models or models where the dark sector states are pair produced.

(iii) A vertex with four or more tracks, which would capture hadronic decays or decays to $\tau^+\tau^-$.  

(iv) A single, nonpointing vertex with one muon with moderate $p_T$, which can record decays of heavy neutral leptons.

We leave these and other possibilities for future work.

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APPENDIX: ADDITIONAL FIGURES

Figure 8 shows the correlation between the inverse track radius and the transverse impact parameter of the fake tracks, for tracks that are reconstructed.
In Fig. 9 we show the trigger efficiency as a function of the truth-level \( R_T \), after imposing (truth-level) acceptance cuts on the \( p_T \) and \( \eta \) range for both muons. For higher masses and high \( R_T \), the higher opening angle between the muons implies that the stubs are more likely to fail the cut on the pitch, such that insufficient stubs are found to reconstruct the track. At low radii, the \( m_\phi = 0.5 \) GeV benchmark point loses efficiency faster due to the \( d_0 \) cut on the tracks.

Finally, with Fig. 10 we also include the distribution of the impact angle in the longitudinal direction. If the primary vertex can be identified, a cut on this variable can further reduce the fake background to the extent that it becomes negligible compared to \( K_\Sigma \) decays.


[19] M. Williams (private communication).