HIGH-GRADIENT LINAC STUDIES IN THE FREQUENCY RANGE OF CLIC

Gilbert GUIGNARD

Abstract

The present status of research and development for high-gradient linacs required for future linear colliders is described. The interval of RF frequency considered here ranges from about 10 GHz to 30 GHz and many studies made for NLC (Next Linear Collider) proposed at SLAC, KEK and IHEP as well as for CLIC (CERN Linear Collider) are covered. After a brief recall of the reason for operating at high frequency when high accelerating gradient is required, major issues are addressed. Effects of strong wake fields on the energy spread at the linac exit and on transverse beam stability, as well as possible compensations are summarized. Consequences for multibunch dynamics are also discussed, together with suggested remedies. The difficult question of the alignment tolerances is approached to underline the necessity of a very efficient scheme of trajectory correction, and the state of the art in building accelerating structure prototypes is given. Prospects for microwave klystrons as high-power RF sources for normal-conducting electron and positron linacs in NLC are briefly described. Finally, recent results concerning the CLIC scheme for generating the necessary power, based on a two-stage accelerator, are presented.


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ABSTRACT

The present status of research and development for high-gradient linacs required for future linear colliders is described. The interval of RF frequency considered here ranges from about 10 GHz to 30 GHz and many studies made for NLC (Next Linear Collider) proposed at SLAC, KEK and IHEP as well as for CLIC (CERN Linear Collider) are covered. After a brief recall of the reason for operating at high frequency when high accelerating gradient is required, major issues are addressed. Effects of strong wake fields on the energy spread at the linac exit and on transverse beam stability, as well as possible compensations are summarized. Consequences for multibunch dynamics are also discussed, together with suggested remedies. The difficult question of the alignment tolerances is approached to underline the necessity of a very efficient scheme of trajectory correction, and the state of the art in building accelerating structure prototypes is given. Prospects for microwave klystrons as high-power RF sources for normal-conducting electron and positron linacs in NLC are briefly described. Finally, recent results concerning the CLIC scheme for generating the necessary power, based on a two-stage accelerator, are presented.

ACCELERATING GRADIENT AND RF FREQUENCY

The total average RF power that is required in one linac is given by

\[ P_{RF} = \frac{P_b}{g^2 \eta} \]  

(1)

where \( g^2 \) is the filling efficiency of the accelerating sections (i.e. the fraction of input energy left at the end of the fill time \( \tau_0 \)) and \( \eta \) the fractional energy extraction by the beam.\(^1\) The beam power \( P_b \) is proportional to the final particle energy \( eU \), the number \( N \) of particles in the beam and the repetition rate \( f_{rep} \),

\[ P_b = eUNf_{rep} \]  

(2)

while the fraction of stored energy extracted by a charge \( Ne \) is given by

\[ \eta = \frac{NeZ_0\omega_0^2}{2\pi c E_0} \]  

(3)

The quantity \( Z_0 \) is frequency-independent and only depends on the shape of the accelerating structure; it is the shunt impedance over Q factor per RF wavelength and is related to the shunt impedance over Q factor per unit length \( r_0^\prime \) via
\[ \omega_0 Z_0 = 2\pi c \eta_0 \] (4)

The wave number \( \omega_0 \) is equal to \( 2\pi \) times the RF frequency \( f_0 \), and \( E_0 \) stands for the accelerating gradient.

Since a high-energy extraction is desirable, the expression (3) advocates for high RF frequencies at a given beam charge. In particular, when aiming at very high gradients in order to limit the total length of the linac, very high frequencies \( f_0 \) are required. The highest possible value is eventually limited by the manufacturing and alignment tolerances as well as the wake fields, and this limit constrains the gradient \( E_0 \) actually attainable.

Other constraints on \( E_0 \) come from the difficulty in generating the required power. The peak power per unit length \( \dot{P} / L_0 \), in a structure of shunt impedance per unit length \( R'_0 \) is indeed given by

\[ \frac{\dot{P}}{L_0} = \frac{E_0^2}{g^2 R'_0 \eta_2} \] (5)

where \( \alpha \) is the power flow attenuation constant and \( \eta_2 \) is the efficiency of the energy transfer from the source to the linac structure. The power requirements (5) related to the desired \( E_0 \) may be large and it is a challenge to develop power sources delivering the necessary energy and working at high frequency.

The scaling of \( E_0 \) with \( \omega_0^2 \) suggested above keeps constant the fraction \( \eta \) and the average power \( P_{RF} \), by virtue of Eqs. (1)–(3). In these conditions the peak power per unit length \( \dot{P} / L_0 \) is proportional to

\[ \frac{\dot{P}}{L_0} \sim \omega_0^{-1/2} E_0^2 \sim \omega_0^{7/2} \] (6)

which includes the fact that \( R'_0 \) varies with \( \sqrt{\omega_0} \).

Increasing \( E_0 \) in this way can be considered until a limit either on the manufacturing tolerances or on the development of power sources is reached, as mentioned already.

A third limitation may arise from the wake fields whose peak values depend on \( \omega_0 \), the iris aperture \( a \) and the loss factor \( k_0 \) as follows,

\[ \tilde{W}_T^\delta \sim \frac{k_0}{\omega_0 a^2} - \frac{R_0}{Q_0 a^2} \sim \frac{\omega_0}{a^2} - \omega_0^3 \]

\[ \tilde{W}_L^\delta \sim k_0 \sim \frac{\omega_0 R_0}{Q_0} \sim \omega_0^2 \] (7)

The rapid increase of the point-charge wakes (mainly transverse) with \( \omega_0 \), and the concomitant beam blow-up are the sources of this limitation.
Since both the achievable gradient and the detrimental effects increase with $\omega_0$, the choice of the RF frequency results from a compromise. The frequency range considered in this study report goes from about 10 GHz to 30 GHz, while the accelerating gradient is supposed to be between 50 and 100 MV/m. This corresponds to linacs suitable for either CLIC (CERN Linear Collider using a Drive Linac) or NLC (Next Linear Collider using pulsed RF generators) as envisaged at SLAC, KEK or IHEP. Table I gives considered values of the parameters discussed above, for the different proposals.

Table I. Examples of parameters.

<table>
<thead>
<tr>
<th></th>
<th>$E_0$ (MV/m)</th>
<th>$\omega_0$ (GHz)</th>
<th>$\hat{P} / L_0$ (MW/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CLIC</td>
<td>80–100</td>
<td>30.0</td>
<td>150</td>
</tr>
<tr>
<td>NLC: SLAC (NLC)</td>
<td>50</td>
<td>11.4</td>
<td></td>
</tr>
<tr>
<td>KEK (JLC)</td>
<td>100</td>
<td>11.4</td>
<td>60–240</td>
</tr>
<tr>
<td>IHEP (VLEPP)</td>
<td>100</td>
<td>14.0</td>
<td></td>
</tr>
</tbody>
</table>

WAKE FIELDS AND SINGLE-BUNCH DYNAMICS

As mentioned above, high-current beams induce in a high-gradient accelerator strong electromagnetic fields that increase rapidly with the RF frequency. These wake fields are responsible for energy loss, energy spread and transverse blow-up. Longitudinal wakes directly influence the distribution of energy inside the bunch, its contribution diminishing the accelerating field seen by the particles. Since these wakes are not uniform within a bunch, the energy loss is accompanied by an energy spread that induces variation of the focusing strength and dispersion of the trajectories inside the bunch in the presence of external magnetic quadrupoles. Transverse wakes deflect parts of the bunch and these deflections depend on the particle momentum and position with respect to the accelerator axis. Because of the energy spread and trajectory dispersion, dipole wakes produce kicks changing along the bunch and eventually producing an apparent beam blow-up (the "head" of the bunch deflecting the "tail"). Quadrupole wakes may also be present but they have been either considered as negligible or not yet studied in the different proposals.

Some compensation of the energy spread $\sigma_E$ using wake potential versus RF sine wave is possible to high orders.\(^1\)\(^2\) This is strongly desirable if the momentum acceptance at the exit of the linac is limited, as for instance in a final-focus system that typically accepts a $\Delta p/p$ of ±2% to ±5%. The total accelerating gradient seen by a particle at position $z$ in the bunch can be written:

$$G(z) = G_{RF} \cos(\omega_0 \frac{z}{c} - \phi_0) - W_L(z)$$  \hspace{1cm} (8)
and the balance between the RF wave and the longitudinal wake will obviously
depend on the phase $\phi_0$, but also on the bunch charge $N$ and bunch length $\sigma_z$ that
enter in $W_L$. Knowing $G(z)$ it is possible to find $\phi_0$ and $\sigma_z$ values which minimize the
spread $\sigma_E$ for a given $N$. Furthermore, the energy distribution $v(E)$ can be calculated\(^2\) in order to study its properties and dependence on $G_{RF}$, $\phi_0$, $\sigma_z$ and $N$, by using

$$v(E) = \frac{1}{N} \frac{dN}{dE} = \frac{1}{N} \frac{dN}{dz} \frac{dE}{dE/dz} = \frac{\rho(z)}{\rho(z) / dz}$$

(9)

where $\rho(z)$ is the charge distribution (Gaussian). Results concerning CLIC are given
as examples.\(^2\) Figure 1 shows $G(z)$ for different charges $N$ with $\phi_0 = 7–8.5^\circ$ and
$\sigma_z = 0.14–0.17$ mm. Figure 2 gives the corresponding energy distributions for $N = 5 \times 10^9$ and $6 \times 10^9$ per bunch. The flatter $G(z)$, the smaller $\sigma_E$, and, in these two
cases, the values obtained are about $4.6\%$ and $7.7\%$ respectively (in the absence of
truncation of $v(E)$). Note also that this adjustment ends up with a minimal tail
population and a somewhat narrow core size (Fig. 2).

![Diagram](image)

Fig. 1. Total gradient minimizing the energy spread $\sigma_E$.

Transverse instabilities due to dipole wakes are all the more critical the smaller
the emittance. In the linac of colliders, the vertical emittance may be very small since
the beam is usually flat. Having a flat beam or a large aspect ratio $R = \sigma_x/\sigma_y$ at the
collision point reduces the average energy loss due to synchrotron radiation. This
energy degradation due to beamstrahlung induces a large energy spread, that should not, however, exceed the energy spreading related to background processes (imposing a limit of $\sim 5\%$ for tolerable $\sigma_E$ from beamstrahlung). Furthermore, a large
Fig. 2. Energy distribution minimizing $\sigma_E$ for $N = 5\times10^9$ and $6\times10^9$.

ratio $R$ allows the avoidance of an excessive repetition rate that varies for constant luminosity and beam–beam radiation $\sigma_E$ as follows:

$$f_{\text{rep}}(R) = f_{\text{rep}}(R = 1)\frac{4}{RH_y}$$ (10)

where $H_y$ is the vertical pinch enhancement factor (typically between 2 and 2.5). For these reasons, values of $R$ and normalized vertical emittance $\gamma \varepsilon_y$ are respectively large and small in the proposals quoted (Table II).

Table II. Beam aspect ratio at final focus and $\gamma$-emittance.

<table>
<thead>
<tr>
<th></th>
<th>$R$</th>
<th>$\gamma \varepsilon_y$ (rad m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CLIC</td>
<td>10–20</td>
<td>2\times10^{-7}</td>
</tr>
<tr>
<td>NLC</td>
<td>100</td>
<td>3\times10^{-8}</td>
</tr>
</tbody>
</table>

The presence of strong dipole wakes (almost 20 times larger in CLIC than in NLC) implies large kicks originating from misalignments of the structure and off-centred trajectories. The corresponding equation of the transverse motion of single particles is given by

$$y'' + k_0^2 y = \left[ k_0^2 - k^2(z,s) \right] y + \frac{\rho}{\gamma} \int_{-\infty}^{Z} \rho W(z^*) y(z^*,s) \, dz^*$$ (11)
where $k^2$ characterizes the linac focusing ($k_0^2$ being its "average" value, independent of $z$) and the wake-field effect is integrated over the heading part of the bunch of charge distribution $\rho$. To counteract this effect, the idea consists of obtaining a coherent motion by imposing the same oscillation period to all particles. This condition, called autophasing, by its author,³ comes directly from inspecting Eq. (11):  

$$k^2(z,s) = k_0^2 + \frac{1}{\gamma} \int_{-\infty}^{z} \rho W_T(z^* - z) \, dz^*$$  

(12)

All the proposals for high-gradient, high-frequency linear accelerators strive to satisfy condition (12) or its linearized version⁴

$$\left. \frac{\partial k^2}{\partial z} \right|_{z=0} = \frac{1}{\gamma} \left( \frac{\partial W_T}{\partial z} \right)_{z=0}$$  

(13)

to limit beam blow-up. There are basically two ways for achieving this variation of the focusing strength with the position $z$ inside the bunch:

1) Using the external focusing of a magnetic FCDO lattice, the change of $k^2$ with $z$ can be obtained via an imposed energy spread $\sigma_{BNS}$, since $k^2 = k_0^2 / \rho p$ if $p$ is the particle momentum. The required energy spread may come in turn from the dependence on $z$ [Eq. (8)] of the accelerating gradient $G$ combined with an adjustment of $\phi_0$. A negative phase $\phi_0$ is needed to ensure that the bunch tail is more focused than the head, according to Eq. (12). The subsequent $\sigma_{BNS}$ ensuring stability is as large as 5% in CLIC, but only 0.2–0.6% in NLC proposals (in proportion to their wake fields). Note that this requirement conflicts with the minimization of $\sigma_E$ discussed above and based on a positive phase $\phi_0$, in particular for high-RF frequency linacs.

2) An elegant way to avoid the conflict with $\sigma_E$ minimization and simultaneously create the spread in $k^2$ without the detour of a large energy spread does exist. It consists of generating part of the transverse focusing directly from RF fields oscillating at the frequency of the accelerating fields, in so-called microwave quadrupoles.⁵ Since the radial electric field in a narrow slit vanishes in the mid-plane, the effective magnetic gradient due to the axial electric field and deduced from Maxwell's equations is given by⁵

$$G_m(T / m) = \frac{\pi}{c \lambda_{RF}} E_0 (MV / m) \sin \phi_1$$  

(14)

where $E_0$ is the peak accelerating gradient, $\lambda_{RF}$ the RF wavelength and $\phi_1$ the RF phase angle measured from the top. In the direction perpendicular to the slit, the electric field is doubled (compared with circular aperture) and overcompensates the
magnetic gradient by exactly a factor 2, thus forming a quadrupole. In practice an oval cavity with circular aperture (Fig. 3) is preferred to a circular cavity with slotted iris, in order to have the required radius and surface finish at the aperture.

Fig. 3. Microwave quadrupole cell with flat cavity (CLIC).

In CLIC, where transverse wakes are large, it is proposed to generate the spread of $k^2$ with microwave quadrupoles using a phase $\phi_1$ close to the phase $\phi_0$ that minimizes $\sigma_E$, i.e. running near the maximum accelerating voltage. In this solution, the main basic focusing $k_0^2$ is created by external magnetic quadrupoles, while the microwave quadrupoles are only responsible for the variation $k_2^2 - k_0^2$ (Fig. 4). Hence, transverse instabilities can be damped (Fig. 5) keeping the energy spread low.
Fig. 4. Equivalent microwave gradient versus the phase.

Fig. 5. Example of blow-up control with microwave quadrupoles and minimum $\sigma_E$. 
WAKE FIELDS AND MULTIBUNCH DYNAMICS

Accelerating long bunch trains that extend over a period comparable to the filling time $\tau_0$ of a cavity section may provoke instabilities of the whole train along the linac, due to interactions with RF fields. The shape, timing and modulation of the RF pulse, as well as long-range longitudinal wake field, are responsible for bunch-to-bunch energy variations. The subsequent energy spread can cause filamentation and emittance growth beyond the acceptance at the exit of the linac. Interactions with resonant transverse electromagnetic fields in disk-loaded waveguides, in particular with the so-called HEM$_{11}$ dipole modes, produce increasing deflections along the bunch train that drive a transverse instability, called beam break-up.

The bunch-to-bunch energy variation produces effects that are more severe with long trains. The fundamental mode, as well as high-order modes of longitudinal wakes, is at the origin of inter-bunch beam loading and the actual RF pulse influences the energy spectrum. There is consequently a need to control bunch-to-bunch energy spreads and some compensation schemes have been studied.\textsuperscript{7,8}

1) Matched filling, i.e. adjustment of the injection timing of the bunch train with respect to the RF pulse and appropriate choice of the bunch spacing. The idea is to have sufficient extra energy in the RF section fill between bunches to cope for the energy lost in accelerating the preceding bunches.

2) Staggered timing, i.e. delay of a subset of klystrons so that some accelerating sections are only partially filled during build-up of the beam-loading voltage to its steady-state value. The number of delayed klystrons is selected to produce a voltage equal to about twice the steady-state beam-loading voltage in the linac.

3) Modulation of RF input, i.e. phase adjustments or small klystron variations during the time when the bunch train is passing through a cavity section. This makes use of the propagation out of the section of the leading edge of the pulse while the train is passing over.

The results of such compensation schemes depend on the bunch length with respect to the section filling-time and on the bunch separation. In the NLC for instance,\textsuperscript{7} the first method applies preferably to short trains (10 bunches of $10^{10}$ particles/bunch, lasting about 10% of $\tau_0$). Figure 6 shows the energy deviation obtained with bunch separation of 16 RF wavelength, 5ns RF pulse rise-time and dispersion of RF frequency components. The fractional energy deviation remains below about 3% but $\sim$75% of the maximum accelerating gradient is used. With long trains (70 bunches or more), the second method seems more appropriate and Fig. 7 shows results obtained in the same conditions of rise-time and dispersion. If the total energy deviation is about the same, only $\sim$65% of the maximum gradient (assumed to be 50 MV/m) is available. Multibunch dynamics in CLIC has not yet been studied.
Fig. 6. Fractional energy deviation in a short train after matched filling.\textsuperscript{7}

Fig. 7. Fractional energy deviation in a long train after staggered timing.\textsuperscript{7}
Performance might probably require only 2–4 bunches per beam separated by 10–20 \( \lambda_{\text{RF}} \) (\( \lambda_{\text{RF}}/c \equiv 33 \) ps) while the RF section filling-time is 11.1 ns. Hence, the first method seems applicable but this must still be checked.

Cumulative beam break-up due to long-range dipole modes of transverse wake fields can be severe. The transverse beam modulation is carried along the linac from accelerating section to accelerating section, through the beam. Blow-up then occurs and manifests itself along the linac as an amplitude growth from the head to the tail of the bunch train. Two possible cures have been investigated:9,10,11

1) damped structures; modified disk-loaded waveguides in which the power of the wake field modes is coupled out to lossy regions through radial slots in the disks and/or azimuthal rectangular waveguides, whereby the external Q-factor of the undesirable HEM mode is lowered to values typically below 20. This was studied in SLAC and KEK, the latter requiring Q-values between 15 and 70 for the predominant TM_{11} modes\(^{12}\) (in order to limit the emittance growth within a factor \( \sqrt{2} \) and alignment tolerances within 80 \( \mu \)m). The limitation of this method might come from the low Q-values required and the large number of cells involved, the practical difficulties increasing with the RF frequency.

2) staggered tuning,\(^9\) variation in the cell dimensions in each accelerating section resulting in a cell-to-cell spread (by a few per cent) of the dipole mode frequencies. These modes are split into \( N_f \) frequency-components, whose distribution can be varied. The best frequency distribution seems to be a truncated Gaussian, since the initial roll-off of the wake is strong, with low partial recoherence within the length of a (short) bunch train.

Whilst the fabrication of damped structures has been tested,\(^{11}\) the possibility of staggered tuning has been investigated by numerical simulations\(^{13}\) and experimental measurements.\(^{14}\) They concern a detuned 50-cavity disk-loaded structure with iris diameter ranging from 0.83 cm to 1.22 cm and Gaussian HEM frequency population centred at 14.45 GHz for a standard deviation of 1.07 GHz. The Advanced Accelerator Test Facility at Argonne makes it possible to measure the energy variation and the horizontal position of a witness bunch following the driving bunch in a time interval between 0 and 1 ns. The former yields the longitudinal wake potential and the latter gives the transverse potential as the structure is swept horizontally. Figure 8 compares calculation with experiment\(^{14}\) and confirms roll-off expectation in this particular case, though it is not clear if recoherence takes place at larger distances \( z \) from the driving bunch (in NLC bunch separation is about 4 cm and a “short” train would cover \( \sim 3.5 \) m). No emittance blow-up simulations are known to the author for RF frequencies between 10 and 30 GHz, but the gain expected from staggered tuning can be illustrated by simulation results\(^{15}\) obtained with 180 bunches, at lower frequency (3 GHz) and with \( N_f = 25 \) (Fig. 9). The
effectiveness of staggered tuning is visible from the fact that without it about half of the bunches have too large amplitudes at the end of the linac, and from the difference in the scale used for the top picture (mm) and for the bottom one (µm).

Fig. 8. Calculated and measured transverse wake potential for a detuned 50-cavity structure.\textsuperscript{14}
Fig. 9. Transverse bunch offsets at linac end, without (a) and with (b) staggered tuning.\textsuperscript{15}

CONSTRAINTS ON THE FABRICATION OF ACCELERATING SECTIONS

The requirement for high gradient at high frequency calls for tight tolerances in the fabrication of the accelerating cavities. Approximately the same principles have been adopted in the design of the accelerator sections proposed at CLIC and at the JLC or VLEPP versions of NLC. The most promising manufacturing method, tested at CLIC, is the brazing of machined copper cups, and the construction of prototypes of CLIC structures\textsuperscript{16} proved that this technique could be successfully acquired by industry.

For the CLIC 30-GHz structure, the tolerances on the cell dimensions (iris diameter of 4 mm and cell diameter of 8.7 mm) are of the order of 2–5 µm (in order to limit the total phase error to 5° over a section) and on the surface finish of about
0.05 μm (to obtain 95% of the nominal Q-value). The high-precision copper cups were made on Pneumo diamond-tool lathes, with laser interferometric feedback with 25 nm resolution. The machining accuracy consistently achieved by manufacturers would eliminate the need for dimple tuning, since the phase shift error was approximately 0.1°/cell. High-quality brazed joints were produced, with two diffusion-bonded annular surfaces at the inside and outer edges of the disks, to prevent braze leakage. Unacceptable frequency changes could be avoided during brazing operations. Complete structures (Fig. 10) with radial holes and vacuum manifolds for pumping and channels for cooling have been manufactured and measurements in the laboratory confirmed the expected parameter values.\(^{16}\) In the JLC design, for example, damping slots could be incorporated in addition.

![Image of a 30 GHz accelerating section (CLIC).](image)

Fig. 10. Finished prototype of a 30 GHz accelerating section (CLIC).

Field-emitted electrons can create multipactoring resonance discharge at well defined field levels, and also dark currents due to the capture, bunching and acceleration of these electrons, eventually producing a parasitic beam. Recently, work was carried out on possible scaling laws\(^ {17}\) for these phenomena with the operating frequency. Basically, both phenomena scale with the frequency \(\omega_0\) for exact geometry scaling, but are influenced by the cavity shape near the axis for the same iris opening \(a\). Working at high frequency with a large iris opening (or large \(a/\lambda_{RF}\) ratio) should be favourable in this respect. Numerical estimates\(^ {17}\) for CLIC cavities at 30 GHz indicate absence of electron capture and dark currents up to a gradient as high as 1400 MV/m. A possible limitation around 100 MV/m seems rather to come from second- or third-order multipactoring, in which emitted electrons lose energy by successive impacts, drift to the outer diameter, and eventually give rise to a breakdown of the structure. Further investigations are needed to better understand these phenomena that already look more critical at the lower end of the frequency interval considered.
TOLERANCE ON THE ALIGNMENT OF LINAC ELEMENTS

The dominant effect associated with misalignments is the blow-up of the projected emittance resulting from the incoherent motions due to transverse dipole wake fields (as already mentioned above). The acceptable growth of the normalized emittance \( \gamma_y \) may vary from only 14% to a factor 3 or 4 depending on the proposal requirements. The subsequent alignment tolerances can be deduced from these numbers assuming first a simple one-to-one trajectory correction aiming at centring the beam in each position monitor (BPM) by moving the preceding lattice quadrupole. To give examples, the corresponding alignment tolerances for CLIC and NLC (SLAC version) are the following (r.m.s. values):

- CLIC: 3 \( \mu \)m on quadrupoles, 5 \( \mu \)m on structures,
- NLC: 7 \( \mu \)m on quadrupoles, 4 \( \mu \)m on structures.

In order to relax these tolerances while keeping the same acceptable emittance growth, a trajectory correction more efficient than the one-to-one method has to be applied. SLAC\(^{18}\) proposed compensating for the dispersion while correcting the orbit and minimizing the wake-field dilutions caused by the corrected trajectory. The minimization procedure developed for achieving this is a weighted least-squares that minimizes the following sum:

\[
\Phi = \sum_{j \in \{\text{BPM}\}} \frac{(\Delta y_{QF})_j^2}{2 \sigma_{\text{prec}}^2} + \frac{(\Delta y_{QD})_j^2}{2 \sigma_{\text{prec}}^2} + \frac{y_j^2}{\sigma_{\alpha}^2 + \sigma_{\text{prec}}^2} = \Phi_{\text{min}}
\]

(15)

where \( y_j \) is the corrected trajectory amplitude, \( \Delta y_{QF} \) the difference trajectory resulting from both QF-variations and corrector adjustments (idem for \( \Delta y_{QD} \), related to QD-variations however), \( \sigma_{\text{prec}} \) is the r.m.s. precision of the BPM readings and \( \sigma_{\alpha} \) the r.m.s. BPM misalignments. Since the QF- and QD-fields are opposite and the QF- and QD-strengths are both supposed to be decreased when measuring \( \Delta y_j \), the sum of these two variation terms mimics the effects of the dispersion (trajectory shift with momentum or quadrupole-strength deviation), while their difference mimics the effects of the wake field (sign depending only on the side where the trajectory is off-centred and not on the quadrupole field polarity). With this algorithm, the NLC (SLAC) alignment tolerances could be relaxed to 70 \( \mu \)m for both the quadrupoles and the accelerating structures. If all the quadrupoles are simultaneously detuned, only one difference \( \Delta y \) corresponding to the dispersion appears in the function \( \Phi \). Minimizing it was called dispersion-free correction while minimizing (15) was termed wake-free correction by its author.\(^{18}\) Figure 11 shows beam distributions after one-to-one, dispersion-free and wake-free corrections in NLC. Plots on the left are projections onto the \( y-y' \) phase plane, while right-hand plots are projections onto the \( y-z \) plane (\( z \): longitudinal coordinate). One sees the strong dilution in (a), reduced to wake-field tail bend in (b) and minimized in (c).
Fig. 11. Beam distributions after one-to-one (a), dispersion-free (b), and wake-free (c) correction in NLC.\textsuperscript{18}

CLIC started from this idea and focused on an achromatic trajectory correction\textsuperscript{19} to higher order, developing the trajectory differences $\Delta y_j$ (measured) and $\Delta Y_j$ (due to corrections) in $\delta = \Delta p/p$,

$$\Delta y_j = \sum \limits_n a_j^n \delta^n, \quad \Delta Y_j = \sum \limits_n A_j^n \delta^n \quad (16)$$

Calling $y_j$ the measured trajectory and $Y_j$ the one due to corrections, the function to be minimized becomes,

$$\Phi = \sum \limits_{j \in \{BPM\}_y} \left\{ w_0 \frac{y_j + Y_j}{\sigma_{\text{at}}^2 + \sigma_{\text{prec}}^2} + \sum \limits_{n=1} w_n \delta^{2n} \frac{a_j^n + A_j^n}{2 \sigma_{\text{prec}}^2} \right\} = \Phi_{\text{min}} \quad (17)$$
where the sum applies to the quadrupoles focusing in the plane considered, in order
to avoid too large a wake dilution. Each variation term of the second sum in Eq. (17)
represents the dispersion order by order. In the applications, second-order corrections
are actually implemented and the arbitrary weights $w_n$ are used to optimize the
results. With this algorithm, the CLIC alignment tolerances could probably be
relaxed to about 5 $\mu$m or more for the quadrupoles and about 10 $\mu$m for the
accelerating structures. The efficiency of this correction is illustrated in Fig. 12
showing a gain of about 3 in the emittance dilution in CLIC, after 12 km, for the
same misalignments (the normalized initial emittance amounts to $0.5 \times 10^{-6}$ rad m).

Fig. 12. Blow-up in CLIC main linac after one-to-one (a)
and achromatic (b) correction.
MICROWAVE KLYSTRONS AS RF POWER SOURCES

Conceptual designs of linacs for future colliders operating around 11 or 14 GHz call for microwave klystrons able to deliver as much as 100–200 MW in pulse lengths of the order of 1 μs. These requirements cannot be satisfied with existing microwave tubes and new klystron designs meet a certain number of challenges briefly recalled hereafter. The maximum power capability is limited by the area available to dissipate beam or RF losses and shrinking with the inverse of $\omega_0^2$. Good power transfer efficiency from the beam to the output circuit and possible release of the intrabeam space charge forces favour high RF voltage $V$ as well as low pervance defined by $I/V^{3/2}$; this implies a large RF gradient across the output gap. Permitting greater beam current $I$ and power makes it necessary to achieve a higher beam convergence that involves better confinement and more precise beam optics. Finally, these high-current, high-voltage conditions increase the risk of failure mechanisms limiting the power; this concerns possible RF breakdowns mainly in the output circuit as well as intrapulse heating due to beam interception, the two mechanisms being interrelated. Typical figures considered are 40–50% for the power transfer efficiency, about 1 or 2 $\mu$A/$V^{3/2}$ for the pervance, beam convergence as high as 200, a gradient lower than 6 MV/cm in the output gap and a scraped beam fraction below 1%.

There are different means envisaged for trying to find solutions. Working at low pervance by increasing $V$ is an important element for beam control, as empirically demonstrated for operational RF sources. Using excellent beam optics near the output circuit and reducing gap voltages by replacing the resonant cavity by multiple gaps or travelling-wave output are possible improvements. The klystron gun voltage can be divided by many intermediate anodes in order to provide the correct potential profile for beam formation and focusing, as in the VLEPP klystron design. In this intricate design (Fig. 13), the beam is composed of many separate "beamlets" produced by different regions of the cathode and is switched by a non-intercepting control electrode (offering the possibility of pulsing the klystron using a quasi-d.c., high-voltage supply and a low-voltage modulator in series with the grid). In order to achieve very low pervance, a "cluster klystron" is proposed by a BNL–SLAC collaboration; it is a collection of 42 separate beams, each comprising a 40-MW klystron and all sharing a common superconducting solenoid. Finally, the use of lumped shavers in order to control beam interception might be necessary.

Some characteristics of high-power klystron development projects, incorporating (separately) the features mentioned, are given in Table III. Achievements so far, as quoted in a recent review paper, are briefly summarized below, together with the reasons for the limitation observed. The SLAC XC klystron achieved 40 MW, 0.8 μs or 72 MW, 0.1 μs pulses (Fig. 14), performance being
limited by RF breakdown in the double-gap output circuit stimulated by beam interception. In the KEK klystron, the output power was restricted to 22 MW by failure of the gun ceramic insulator. In the VLEPP klystron, 50 MW has been achieved, limited by a substantial beam loss that amounts to 70 out of 200 A. The cluster klystron is still at the design stage.
Table III: High-power klystron projects.

<table>
<thead>
<tr>
<th>Klystron</th>
<th>Wavelength (cm)</th>
<th>Power out (MW)</th>
<th>Pulse length (µs)</th>
<th>Voltage (kV)</th>
<th>Microperveance (µA/V^{3/2})</th>
<th>Frequency (GHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SLAC 5045</td>
<td>10.5</td>
<td>67</td>
<td>3.5</td>
<td>350</td>
<td>2.0</td>
<td>2.86</td>
</tr>
<tr>
<td>SLAC</td>
<td>10.5</td>
<td>150</td>
<td>1.0</td>
<td>450</td>
<td>2.0</td>
<td>2.86</td>
</tr>
<tr>
<td>SLAC XC</td>
<td>2.6</td>
<td>100</td>
<td>1.0</td>
<td>550</td>
<td>1.2</td>
<td>11.4</td>
</tr>
<tr>
<td>KEK</td>
<td>2.6</td>
<td>120</td>
<td>1.0</td>
<td>550</td>
<td>1.2</td>
<td>11.4</td>
</tr>
<tr>
<td>VLEPP</td>
<td>2.1</td>
<td>150</td>
<td>1.0</td>
<td>1000</td>
<td>0.3</td>
<td>14.2</td>
</tr>
<tr>
<td>Cluster</td>
<td>2.6</td>
<td>1680</td>
<td>1.0</td>
<td>400</td>
<td>0.4</td>
<td>11.4</td>
</tr>
</tbody>
</table>

DRIVE LINAC AS HIGH-FREQUENCY POWER SOURCE

Owing to difficulties met in the development of microwave klystrons operating in the frequency range of 11–14 GHz, it is unthinkable to use similar tubes to deliver the 30-GHz, ~150 MW/m peak power per unit length required in the CLIC linac structure. The CLIC scheme for generating the necessary power is based on a two-stage accelerator; there is a drive beam that runs parallel to the main beam and ensures power flow to the main linac. The drive linac contains strings of travelling-wave transfer structures, in which short and intense bunches induce the required power that is then fed to the main linac, and sectors of superconducting (SC) cavities supplying energy to the beam when necessary. The use of SC cavities to reboost the drive beam as well as to accelerate it up to its initial energy is dictated by the concern of good extraction efficiency; LEP-type cavities operating at ~ 350 MHz with a gradient of ~ 6 MV/m are considered. The drive-beam energy should be of the order of a few GeV, which implies no longitudinal mixing inside the bunches and no phase slip with respect to the main beam. Owing to the unavoidable intermittent reacceleration, the drive beam has to be arranged in discrete trains of dense bunchlets that all contribute to the build-up of a decelerating field in the transfer structure and are separated by the 30-GHz wavelength. To generate a pulse of length equal to the main structure filling time \( \tau_0 \) (11.1 ns), four such trains are needed, separated by the 350-MHz wavelength. The total charge needed per train is about 1.65 µC and the number of bunchlets per train depends on the matching of the decelerating field build-up to the SC cavity accelerating gradient. Simply minimizing the deviation of the linear build-up from the sinusoidal acceleration wave limits this number to 11, but the use of voltage harmonics schemes (their sum giving almost a linear function as shown in Fig. 15) might allow for 43 bunchlets (with correspondingly lower charge per bunchlet).

This drive-linac conceptual design implies certain challenges which have been addressed, mainly the bunchlet generation, the transfer structure design and the beam
Fig. 15. Accelerating ramp obtained with 3 RF harmonics.

dynamics control. Owing to the difficulty of generating short (1 mm r.m.s.) and dense (up to $10^{12}$ particles) bunchlets, a test facility (CTF) has been built.\textsuperscript{25} It includes an RF gun, a beam line acting as magnetic spectrometer, acceleration to 60 MeV at 3 GHz and RF power generation at 30 GHz (using prototype structures). A charge up to 30 nC per beam should be obtained using a laser-driven photocathode, synchronized with the RF. During first tests using a prototype of the main linac structure instead of an actual transfer structure, a 48-kW power pulse was extracted.

The most recent transfer structure design proposed,\textsuperscript{26} is based on power-collecting rectangular waveguides that run along the outside of the beam pipe (either on each side or above and below) and are coupled to the inside via slits about 0.5 m long (Fig. 16). The phase velocity in the waveguide is adjusted by periodic indentations. Numerical calculations and model work are being carried out in parallel to check the possibility of generating the required flat power pulse and the amplitude of the wake fields. This design must indeed provide the low impedance needed ($\sim 4.5$ $\Omega$/m for $R'/Q$) and the required decelerating field per bunchlet ($\sim 65$ kV/m for a population of $10^{12}$), while minimizing the undesirable wake-field modes that could compromise beam stability. The dynamics of such a beam includes special features: the energy differences between bunchlets are unusually large owing to the increasing decelerating field, the energy spread within each bunchlet is wide since the bunch length is not short with respect to $\lambda_{RF}$, and the amplitudes of the synchronous wake fields may be disturbing. The impact of these features on the beam transport and
dynamics, in the presence of alignment imperfections, trajectory correction, variable wakes and magnetic focusing, is being investigated by numerical simulations. Figure 17 gives an example of initial- and final-energy distributions in a train of 11 bunches travelling over $\sim 3.5$ km. Phase plots of the emittances (Fig. 18) show that all the bunchlets remain within the beam-pipe acceptance (circle tangent to the frame), with the assumptions retained for this calculation, in particular no synchronous, slowly damped transverse wakes. Further investigations are needed to check the feasibility of the scheme.

Fig. 16. Model of the most recent transfer structure design.

Fig. 17. Initial (0) and final (1) energy distributions in a drive-beam train.
Fig. 18. Bunchlet emittances (H and V) at the drive-linac exit.

CONCLUSIONS

The choice of the RF-frequency in a high-gradient normal-conducting linac will probably fall in the 10–30 GHz interval and result from a compromise between the opposing requirements of saving power and minimizing harmful effects. A lot of studies and simulations improved the knowledge of the mechanisms involved in wake field effects and beam stability in the presence of one bunch or several bunches per beam. They revealed a number of promising correction possibilities aiming at low energy-spread and small transverse emittances at the exit of the linac. The question of the tight alignment tolerances required remains challenging, but looks solvable if good alignment strategies are defined. The idea of using microwave quadrupoles for stabilizing the beam in the presence of strong wake fields has been reinforced by numerical simulations. Model work on high-frequency accelerating structures proved that they could be manufactured by industry and recent studies indicate that the risk of dark currents decreases at higher frequency. Microwave klystrons for 250-GeV and 50-MV/m linacs seem feasible in the near future, as do the companion RF-pulse compression systems. Prospects for the peak power requirements at 500 GeV and 100 MV/m are however more distant, since technical limitations have to be overcome. For the CLIC scheme based on a two-stage accelerator, significant progress has been made on the study of the drive-beam dynamics and the design of the transfer structures. In this case, challenging issues are the generation of the required short and dense bunchlets, and the development of efficient transfer structures that are least harmful to the drive beam.
REFERENCES


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